

FIG. 1

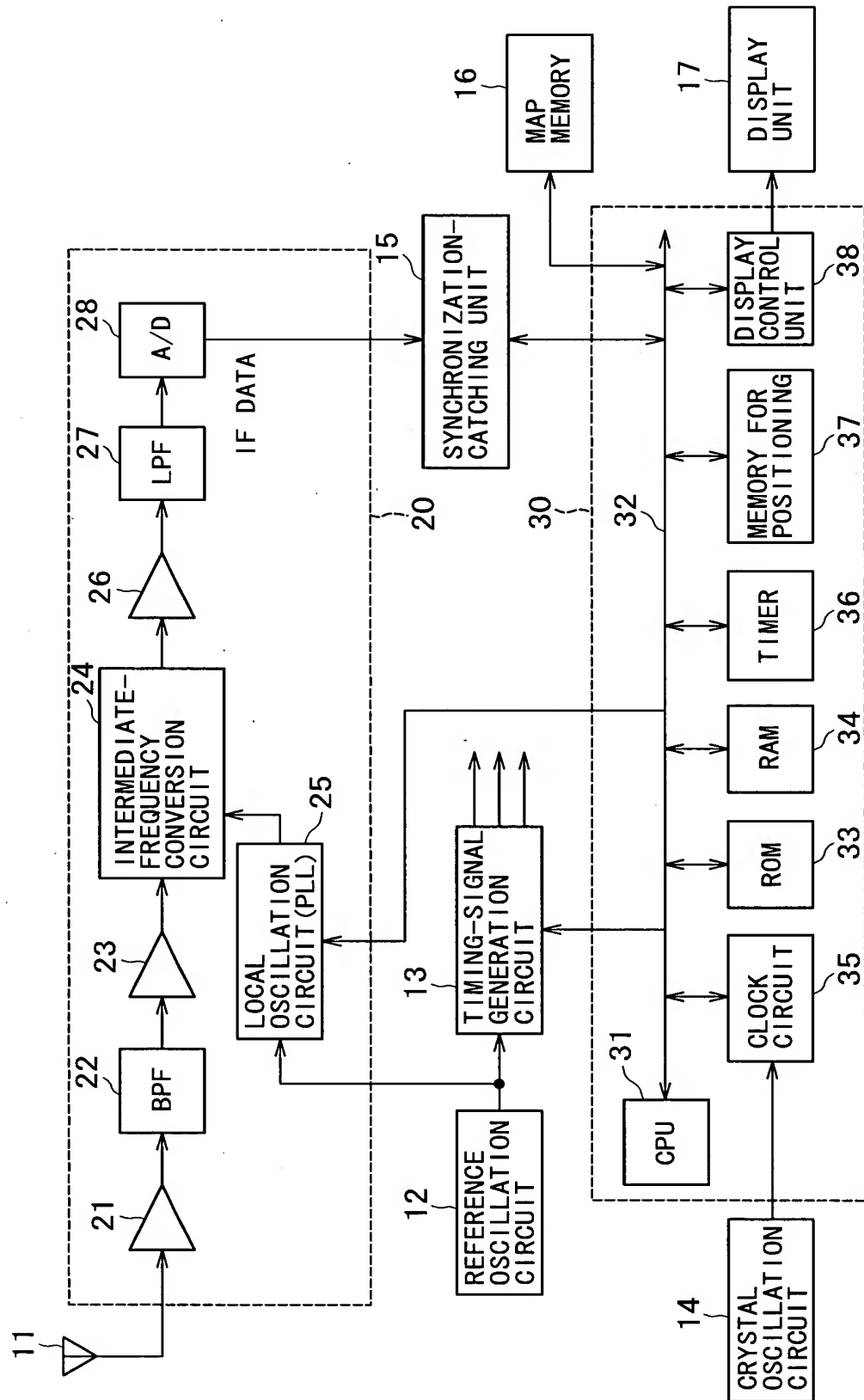


FIG. 2

$$t_i = T_{ci} + T_{mi} \quad \text{..... (1a)}$$

t_i : DIFFUSION-CODE TRANSMISSION TIME

T_{ci} : VALUE OF DIGITS EXPRESSING A NUMBER SMALLER THAN 1 msec

(PHASE OF DIFFUSION CODE)

T_{mi} : VALUE OF DIGITS EXPRESSING A NUMBER EQUAL TO OR GREATER THAN 1 msec

$$t_i = T_{ci} + T_i + t_o \quad \text{..... (1b)}$$

t_i : DIFFUSION-CODE TRANSMISSION TIME

T_{ci} : VALUE OF DIGITS EXPRESSING A NUMBER SMALLER THAN 1 msec (PHASE OF DIFFUSION CODE)

$(T_i + t_o)$: VALUE OF DIGITS EXPRESSING A NUMBER EQUAL TO OR GREATER THAN 1 msec

t_o : REFERENCE TIME (COMMON TO SATELLITES)

T_i : DIFFERENTIAL TIME

F I G. 3

$$f_i(X_o, \tau, t_o) = \begin{vmatrix} X_i(t_i) - X_o & -c \{ (tr - t_i) + \tau \} \\ X_i(T_{ci} + T_i + t_o) - X_o & -c \{ tr - (T_{ci} + T_i + t_o) + \tau \} \end{vmatrix} = 0$$

..... (2)

$$X_i(t_i) = (x_i(t_i) y_i(t_i) z_i(t_i))^T$$

..... (3)

$$X_o = (x_o \ y_o \ z_o)^T$$

..... (4)

$$f_1(X_o, \tau, t_o) = \begin{vmatrix} X_1(T_{c1} + T_1 + t_o) - X_o \\ -c \{ tr - (T_{c1} + T_1 + t_o) + \tau \} \end{vmatrix} = 0$$

..... (2a)

$$f_2(X_o, \tau, t_o) = \begin{vmatrix} X_2(T_{c2} + T_2 + t_o) - X_o \\ -c \{ tr - (T_{c2} + T_2 + t_o) + \tau \} \end{vmatrix} = 0$$

..... (2b)

$$f_3(X_o, \tau, t_o) = \begin{vmatrix} X_3(T_{c3} + T_3 + t_o) - X_o \\ -c \{ tr - (T_{c3} + T_3 + t_o) + \tau \} \end{vmatrix} = 0$$

..... (2c)

$$f_4(X_o, \tau, t_o) = \begin{vmatrix} X_4(T_{c4} + T_4 + t_o) - X_o \\ -c \{ tr - (T_{c4} + T_4 + t_o) + \tau \} \end{vmatrix} = 0$$

..... (2d)

$$f_5(X_o, \tau, t_o) = \begin{vmatrix} X_5(T_{c5} + T_5 + t_o) - X_o \\ -c \{ tr - (T_{c5} + T_5 + t_o) + \tau \} \end{vmatrix} = 0$$

..... (2e)

F I G. 4

POINT OF INTEREST

$$(X_o(n), \tau(n), t_o(n)) \quad \dots\dots (11)$$

$$\begin{aligned} \Delta f_i = & \frac{\partial f_i}{\partial x_o(n)} \Delta x_o + \frac{\partial f_i}{\partial y_o(n)} \Delta y_o + \frac{\partial f_i}{\partial z_o(n)} \Delta z_o \\ & + \frac{\partial f_i}{\partial \tau(n)} \Delta \tau + \frac{\partial f_i}{\partial t_o(n)} \Delta t_o \quad \dots\dots (12) \end{aligned}$$

$$f_i(X_o(n), \tau(n), t_o(n)) + \Delta f_i = 0 \quad \dots\dots (13)$$

$$(\Delta X_o, \Delta \tau, \Delta t_o) \quad \dots\dots (14)$$

$$\Delta X_o = (\Delta x_o \quad \Delta y_o \quad \Delta z_o)^T \quad \dots\dots (15)$$

$$\frac{\partial f_i}{\partial x_o(n)} = \frac{\partial f_i}{\partial x_o} \Big|_{x_o=x_o(n)} \quad \dots\dots (16)$$

$$\begin{aligned} F(X_o(n), \tau(n), t_o(n)) + \Delta F \\ = F(X_o(n), \tau(n), t_o(n)) + J(X_o(n), \tau(n), t_o(n)) \Delta P \\ = 0 \quad \dots\dots (17) \end{aligned}$$

$$F = (f_1 \quad f_2 \quad f_3 \quad f_4 \quad f_5)^T \quad \dots\dots (18)$$

$$\Delta P = (\Delta x_o \quad \Delta y_o \quad \Delta \tau \quad \Delta t_o)^T \quad \dots\dots (19)$$

F I G. 5

$$J(X_o(n), \tau(n), t_o(n)) = \begin{bmatrix} \frac{\partial f_1}{\partial x_o(n)} & \frac{\partial f_1}{\partial y_o(n)} & \frac{\partial f_1}{\partial z_o(n)} & \frac{\partial f_1}{\partial \tau(n)} & \frac{\partial f_1}{\partial t_o(n)} \\ \frac{\partial f_2}{\partial x_o(n)} & \frac{\partial f_2}{\partial y_o(n)} & \frac{\partial f_2}{\partial z_o(n)} & \frac{\partial f_2}{\partial \tau(n)} & \frac{\partial f_2}{\partial t_o(n)} \\ \frac{\partial f_3}{\partial x_o(n)} & \frac{\partial f_3}{\partial y_o(n)} & \frac{\partial f_3}{\partial z_o(n)} & \frac{\partial f_3}{\partial \tau(n)} & \frac{\partial f_3}{\partial t_o(n)} \\ \frac{\partial f_4}{\partial x_o(n)} & \frac{\partial f_4}{\partial y_o(n)} & \frac{\partial f_4}{\partial z_o(n)} & \frac{\partial f_4}{\partial \tau(n)} & \frac{\partial f_4}{\partial t_o(n)} \\ \frac{\partial f_5}{\partial x_o(n)} & \frac{\partial f_5}{\partial y_o(n)} & \frac{\partial f_5}{\partial z_o(n)} & \frac{\partial f_5}{\partial \tau(n)} & \frac{\partial f_5}{\partial t_o(n)} \end{bmatrix} \quad \dots\dots (21)$$

$$\frac{\partial f_i}{\partial x_o(n)} = - \frac{x_i(T_{ci}+T_i+t_o(n)) - x_o(n)}{|X_i(T_{ci}+T_i+t_o(n)) - X_o(n)|} \quad \dots\dots (22)$$

$$\frac{\partial f_i}{\partial y_o(n)} = - \frac{y_i(T_{ci}+T_i+t_o(n)) - y_o(n)}{|X_i(T_{ci}+T_i+t_o(n)) - X_o(n)|} \quad \dots\dots (23)$$

$$\frac{\partial f_i}{\partial z_o(n)} = - \frac{z_i(T_{ci}+T_i+t_o(n)) - z_o(n)}{|X_i(T_{ci}+T_i+t_o(n)) - X_o(n)|} \quad \dots\dots (24)$$

$$\frac{\partial f_i}{\partial \tau_o(n)} = -c \quad \dots\dots (25)$$

$$\frac{\partial f_i}{\partial T_o(n)} = - \frac{(X_i(T_{ci}+T_i+t_o(n)) - X_o(n)) \cdot V_i(T_{ci}+T_i+t_o(n))}{|X_i(T_{ci}+T_i+t_o(n)) - X_o(n)|} + c \quad \dots\dots (26)$$

$$A \cdot B = (X_i(T_{ci}+T_i+t_o(n)) - X_o(n)) \cdot V_i(T_{ci}+T_i+t_o(n)) \quad \dots\dots (27)$$

FIG. 6

INITIAL VALUES

$(X_o(0), \tau(0), t_o(0)) = (X_{oa}, 0, t_{oa})$ (31)

$X_o(0) = X_{oa}$: APPROXIMATE POSITION OF RECEIVER

$\tau(0)$: INITIAL VALUE OF ERROR τ OF RECEIVER INTERNAL CLOCK

$t_o(0) = t_{oa}$: INITIAL VALUE OF REFERENCE TIME t_o

(TIME INDICATED BY INTERNAL CLOCK OF RECEIVER
AT ITERATION COMPUTATION START TIME)

FIG. 7

NEXT POINT OF INTEREST

$$\begin{aligned} & (X_o(n+1), \tau(n+1), to(n+1)) \\ & = (X_o(n) + \Delta X_o, \tau(n) + \Delta \tau, to(n) + \Delta to) \\ & \dots\dots\dots (33) \end{aligned}$$

CONVERGENCE CRITERIA (ε : CONSTANT)

$$|\Delta X_0| < \varepsilon \quad \dots\dots (35)$$

$$|\Delta P| < \varepsilon \quad \dots\dots (36)$$

$$|F(X_0(n), \tau(n), t_0(n))| < \varepsilon \quad \dots\dots (37)$$

F I G. 8

CALCULATION OF DIFFERENTIAL TIME T_i

$$t_1 = T_{c1} + t_o \quad \text{..... (1c)}$$

$$t_i = T_{ci} + T_i + t_o \quad (i \geq 2) \quad \text{..... (1d)}$$

$$T_i = (T_i + t_o) - t_o = (t_i - T_{ci}) - (t_1 - T_{c1}) \quad \text{..... (41)}$$

$$c(t_r - t_i) = |X_i(t_i) - X_o| \quad \text{..... (42)}$$

$$t_i = t_r - \frac{|X_i(t_i) - X_o|}{c} \quad \text{..... (43)}$$

$$t_1 = t_r - \frac{|X_1(t_1) - X_o|}{c} \quad \text{..... (44)}$$

$$T_i = \left(\frac{|X_1(t_1) - X_o|}{c} + T_{c1} \right) - \left(\frac{|X_i(t_i) - X_o|}{c} + T_{ci} \right) \quad \text{..... (45)}$$

$$c \times 1.0 \times 10^{-3} \text{ [m]} \simeq 3.0 \times 10^5 \text{ [m]} \quad \text{..... (46)}$$

$$t_i = t_1 - 2.0 \times 10^{-2} \text{ [SECONDS]} \quad \text{..... (47)}$$

F I G. 9

TOLERANCE OF APPROXIMATE POSITION OF RECEIVER

$$cTi = (|X1(t1) - Xo| + cTc1) - (|Xi(ti) - Xo| + cTci) \quad \text{..... (51)}$$

$$\begin{aligned} & (|X1(t1) - (Xo + \Delta X)| + cTc1) \\ & - (|Xi(ti) - (Xo + \Delta X)| + cTci) \\ & = (|X1(t1) - Xo| + | \Delta X | + cTc1) \\ & - (|Xi(ti) - Xo| - | \Delta X | + cTci) \\ & = (|X1(t1) - Xo| + cTc1) \\ & - (|Xi(ti) - Xo| + cTci) + 2 | \Delta X | \\ & = cTi + 2 | \Delta X | \quad \text{..... (52)} \end{aligned}$$

$| \Delta X |$: DISTANCE BETWEEN COORDINATES
REPRESENTING APPROXIMATE
POSITION OF RECEIVER AND ACTUAL
POSITION OF RECEIVER

$$| A | > | B | \quad \text{..... (63)}$$

$$| A | - | B | \leq | A - B | \leq | A | + | B | \quad \text{..... (64)}$$

$$\begin{aligned} & | Xi(ti) - (Xo + \Delta X) | \\ & = | (Xi(ti) - Xo) - \Delta X | \quad \text{..... (65)} \end{aligned}$$

$$A = Xi(ti) - Xo \quad \text{..... (66)}$$

$$B = \Delta X \quad \text{..... (67)}$$

$$\begin{aligned} & | Xi(ti) - Xo | - | \Delta X | \\ & \leq | (Xi(ti) - Xo) - \Delta X | \\ & \leq | Xi(ti) - Xo | + | \Delta X | \quad \text{..... (68)} \end{aligned}$$

F I G. 1 0

TOLERANCE OF ERROR OF RECEIVER INTERNAL TIME

$$t_1 + \Delta t = t_i + \Delta t + 2.0 \times 10^{-2} \text{ [SECONDS]} \quad \text{..... (53)}$$

$$\begin{aligned} & (| X_1(t_1 + \Delta t) - X_o | + cTc_1) \\ & \quad - (| X_i(t_1 + \Delta t) - X_o | + cTc_i) \\ & = (| X_1(t_1 + \Delta t) - X_o | + cTc_1) \\ & \quad - (| X_i(t_i + \Delta t + 2.0 \times 10^{-2}) - X_o | + cTc_i) \\ & = (| X_1(t_1) - X_o | + \Delta t \times 1.0 \times 10^3 + cTc_1) \\ & \quad - (| X_i(t_i) - X_o | - \Delta t + 2.0 \times 10^{-2}) \times 1.0 \times 10^3 + cTc_i) \\ & = (| X_1(t_1) - X_o | + cTc_1) - (| X_i(t_i) - X_o | + cTc_i) \\ & \quad + (2\Delta t + 2.0 \times 10^{-2}) \times 1.0 \times 10^3 \\ & = cTi + (2\Delta t + 2.0 \times 10^{-2}) \times 1.0 \times 10^3 \quad \text{..... (54)} \end{aligned}$$

$$\begin{aligned} \Delta d & = (2\Delta t + 2.0 \times 10^{-2}) \times 1.0 \times 10^3 \text{ [m]} \\ & \simeq 2\Delta t \times 1.0 \times 10^3 \text{ [m]} \quad \text{..... (55)} \end{aligned}$$

F I G. 1 1

$$2 | \Delta X | + 2 | \Delta t | \times 1.0 \times 10^3 < 1.5 \times 10^5 \quad \text{..... (56)}$$

$$| \Delta X | + 1.0 \times 10^3 \times | \Delta t | < 7.5 \times 10^4 \quad \text{..... (57)}$$

F I G. 1 2

SECOND METHOD

$$f1(X_o, \tau, t_o) = \frac{|X1(Tc1+T1+t_o)-X_o|}{-c \{tr-(Tc1+T1+t_o)+\tau\}} = 0 \quad \dots\dots (2a)$$

$$f2(X_o, \tau, t_o) = \frac{|X2(Tc2+T2+t_o)-X_o|}{-c \{tr-(Tc2+T2+t_o)+\tau\}} = 0 \quad \dots\dots (2b)$$

$$f3(X_o, \tau, t_o) = \frac{|X3(Tc3+T3+t_o)-X_o|}{-c \{tr-(Tc3+T3+t_o)+\tau\}} = 0 \quad \dots\dots (2c)$$

$$f4(X_o, \tau, t_o) = \frac{|X4(Tc4+T4+t_o)-X_o|}{-c \{tr-(Tc4+T4+t_o)+\tau\}} = 0 \quad \dots\dots (2d)$$

$$f5(X_o, \tau, t_o) = \frac{|X5(Tc5+T5+t_o)-X_o|}{-c \{tr-(Tc5+T5+t_o)+\tau\}} = 0 \quad \dots\dots (2e)$$

$$f6(X_o, \tau, t_o) = \frac{|X6(Tc6+T6+t_o)-X_o|}{-c \{tr-(Tc6+T6+t_o)+\tau\}} = 0 \quad \dots\dots (2f)$$

$$\Delta P = (J^T J)^{-1} J^T (-F) \quad \dots\dots (61)$$

F I G. 1 3

THIRD METHOD

$$f_5(X_o) = |X_o| - |X_{oa}| = 0 \quad \text{..... (71)}$$

X_{oa} : APPROXIMATE POSITION OF RECEIVER

$$\frac{\partial f_5}{\partial x_o(n)} = \frac{x_o(n)}{|X_o(n)|} \quad \text{..... (72)}$$

$$\frac{\partial f_5}{\partial y_o(n)} = \frac{y_o(n)}{|X_o(n)|} \quad \text{..... (73)}$$

$$\frac{\partial f_5}{\partial z_o(n)} = \frac{z_o(n)}{|X_o(n)|} \quad \text{..... (74)}$$

$$\frac{\partial f_5}{\partial \tau(n)} = 0 \quad \text{..... (75)}$$

$$\frac{\partial f_5}{\partial t_o(n)} = 0 \quad \text{..... (76)}$$

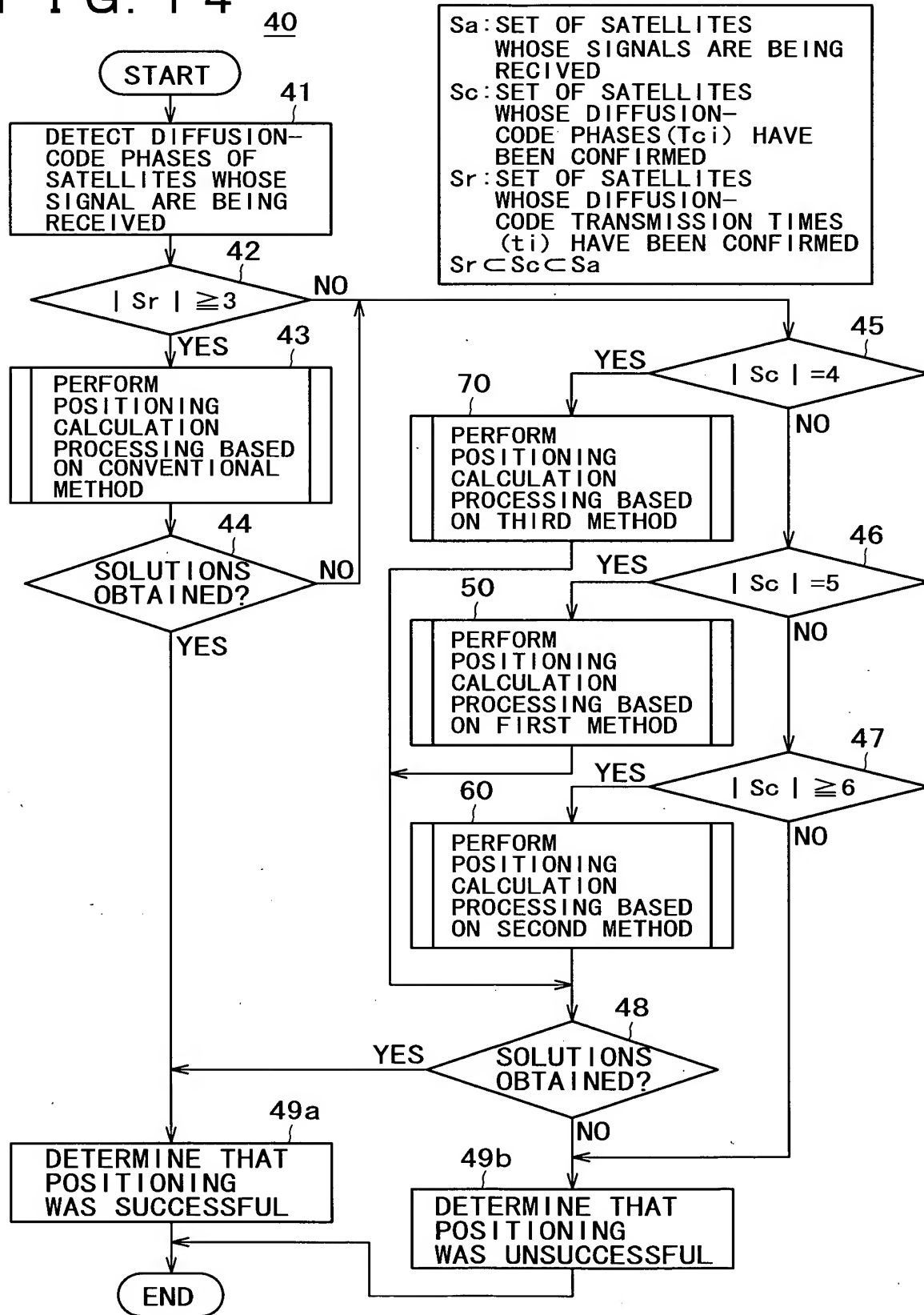


FIG. 15

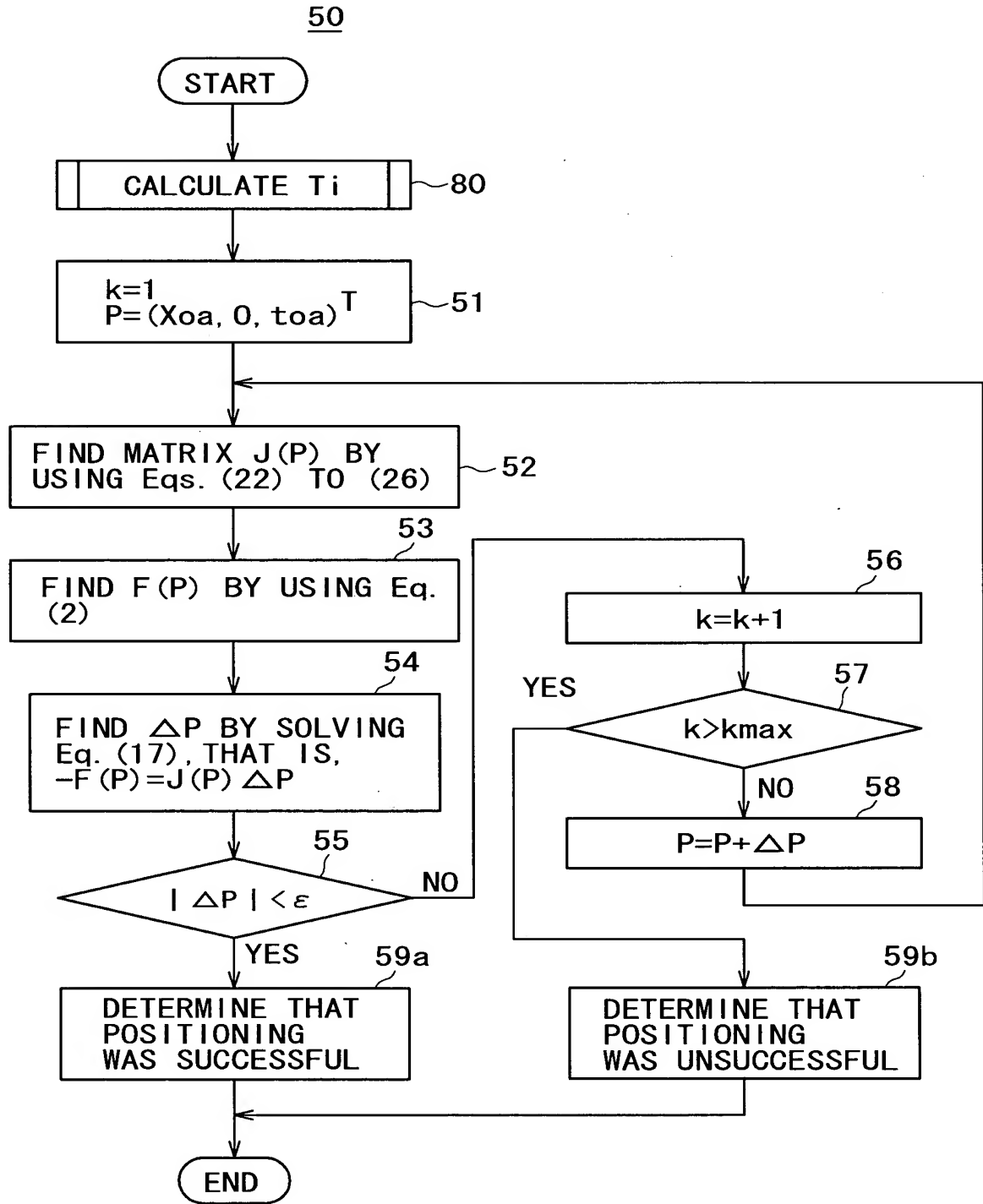


FIG. 16

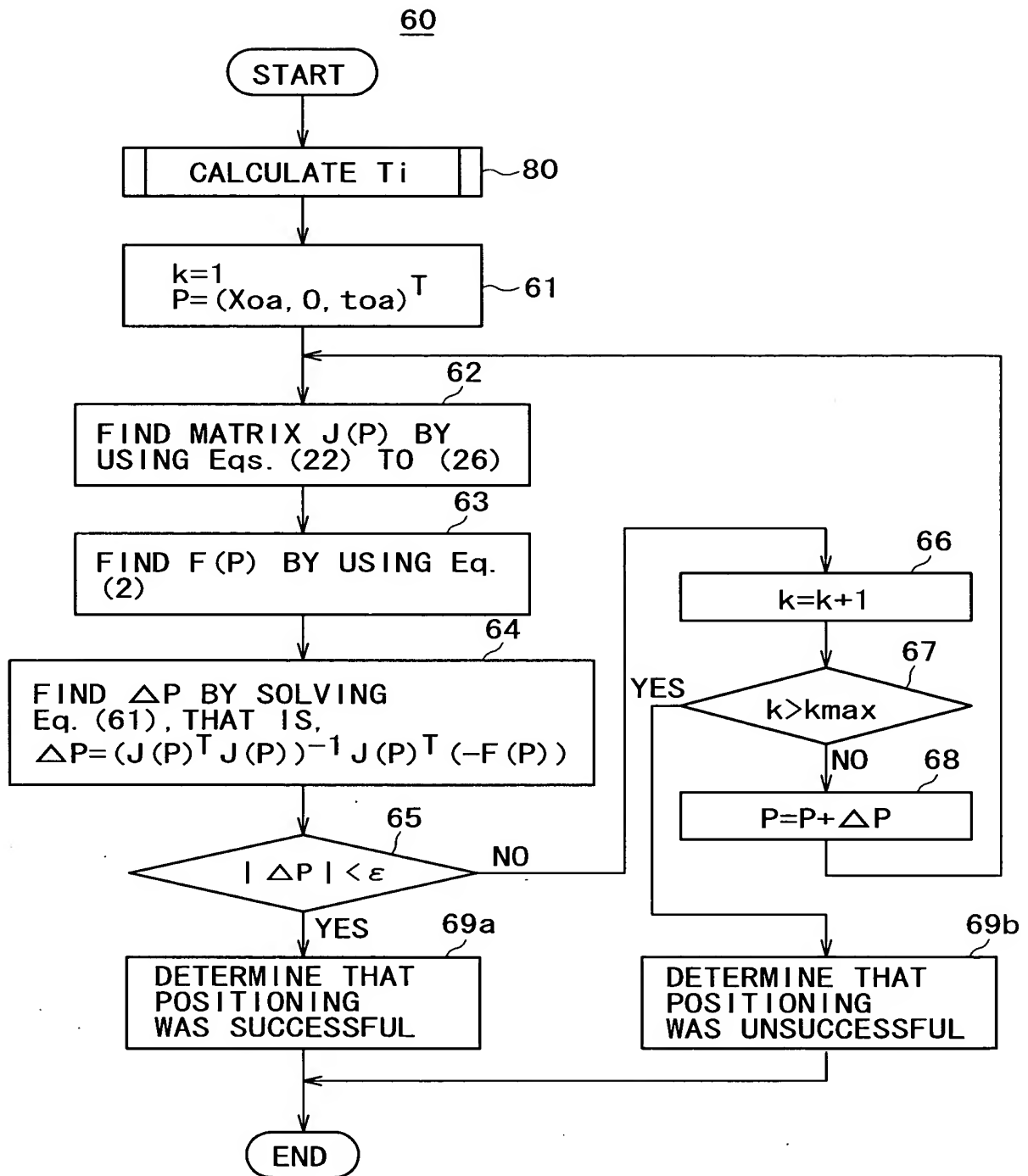


FIG. 17

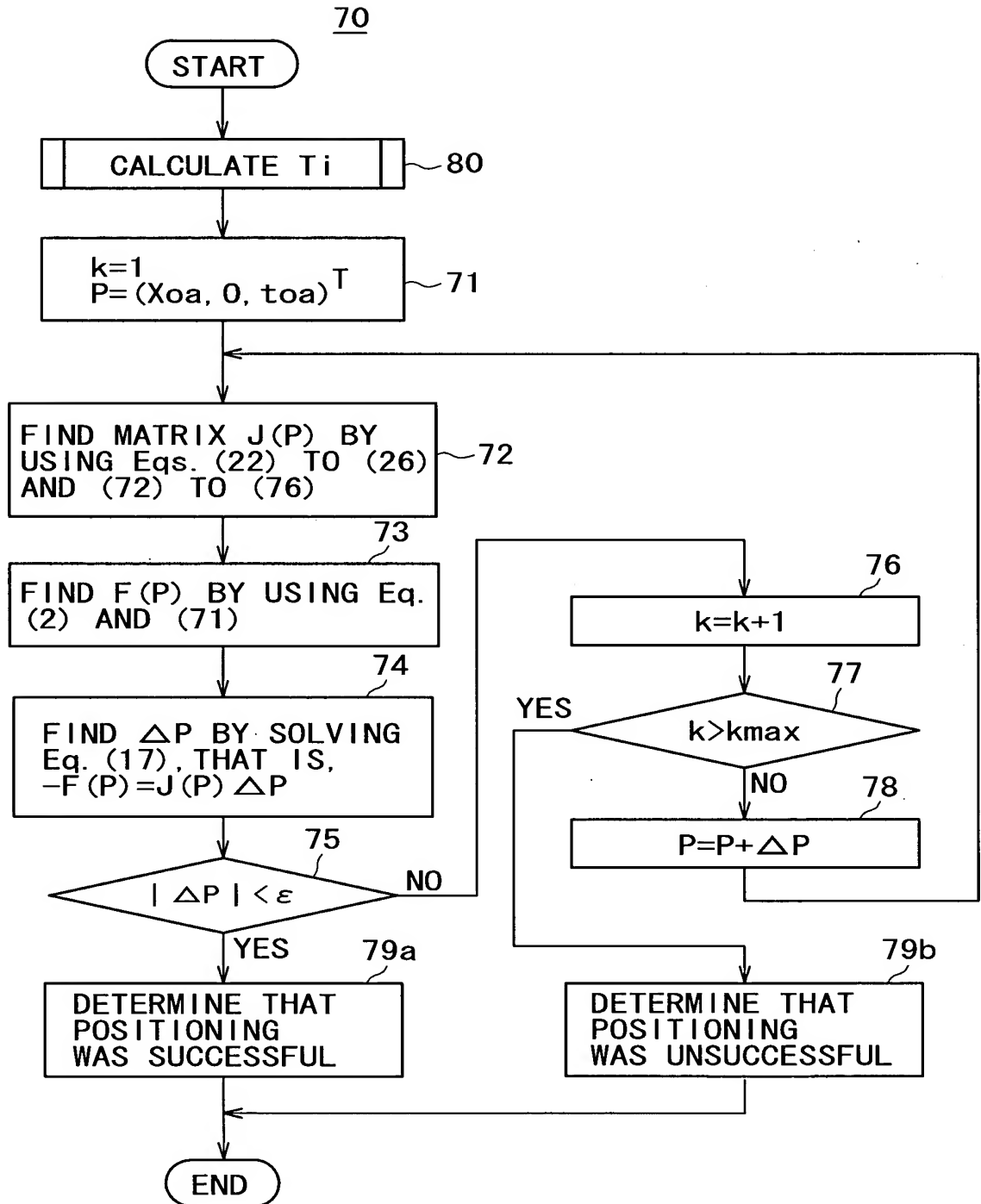


FIG. 18

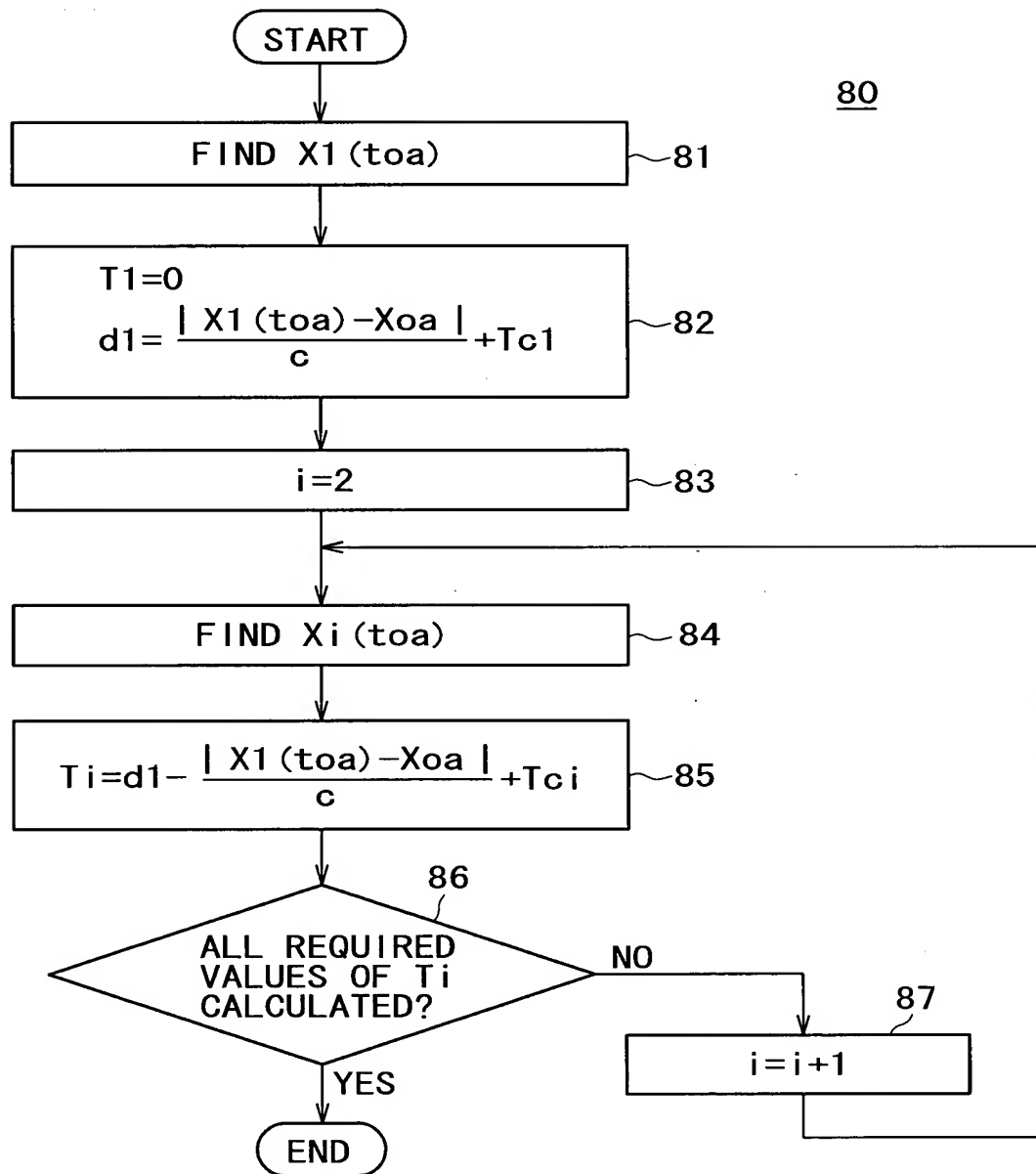


FIG. 19

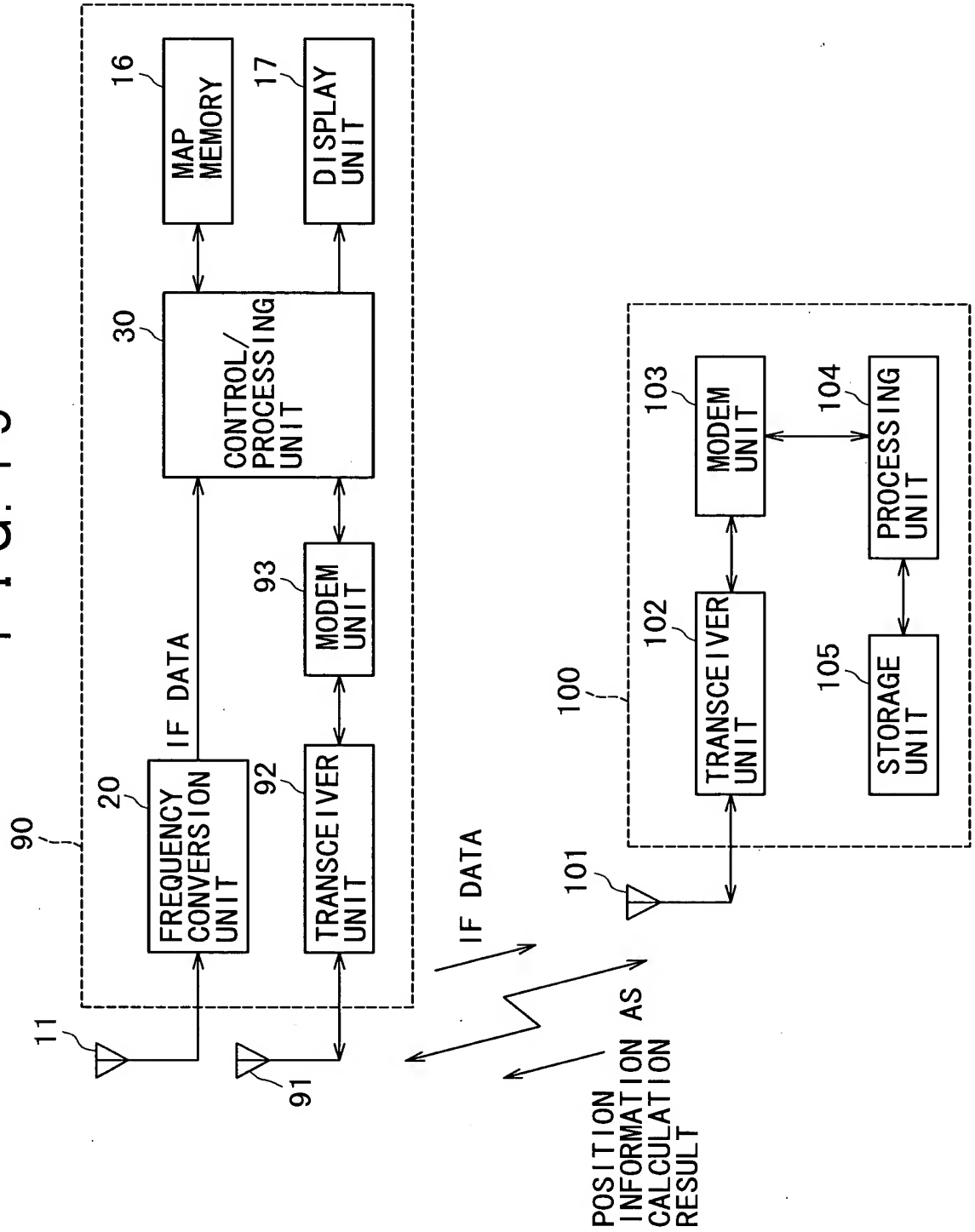


FIG. 20

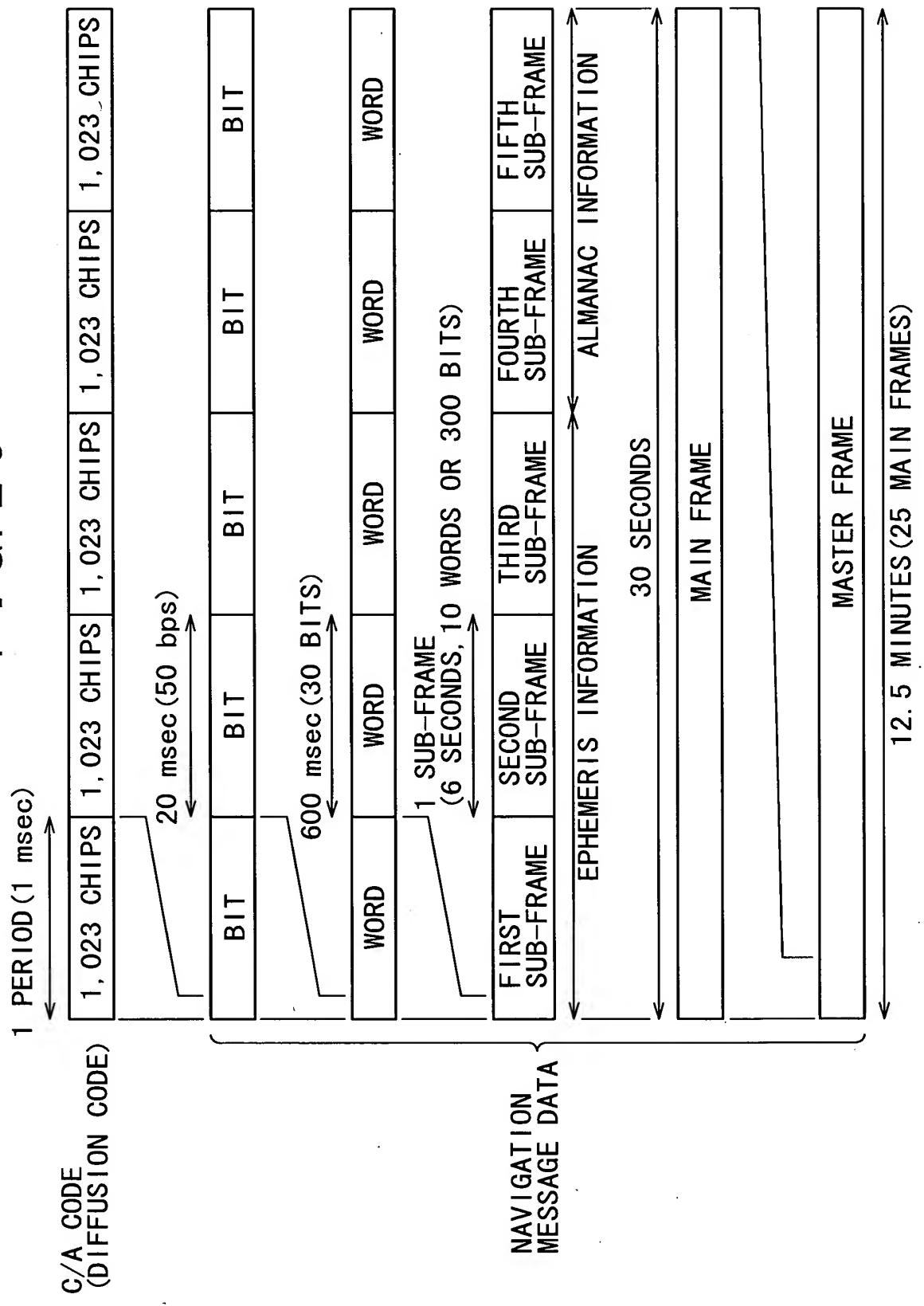
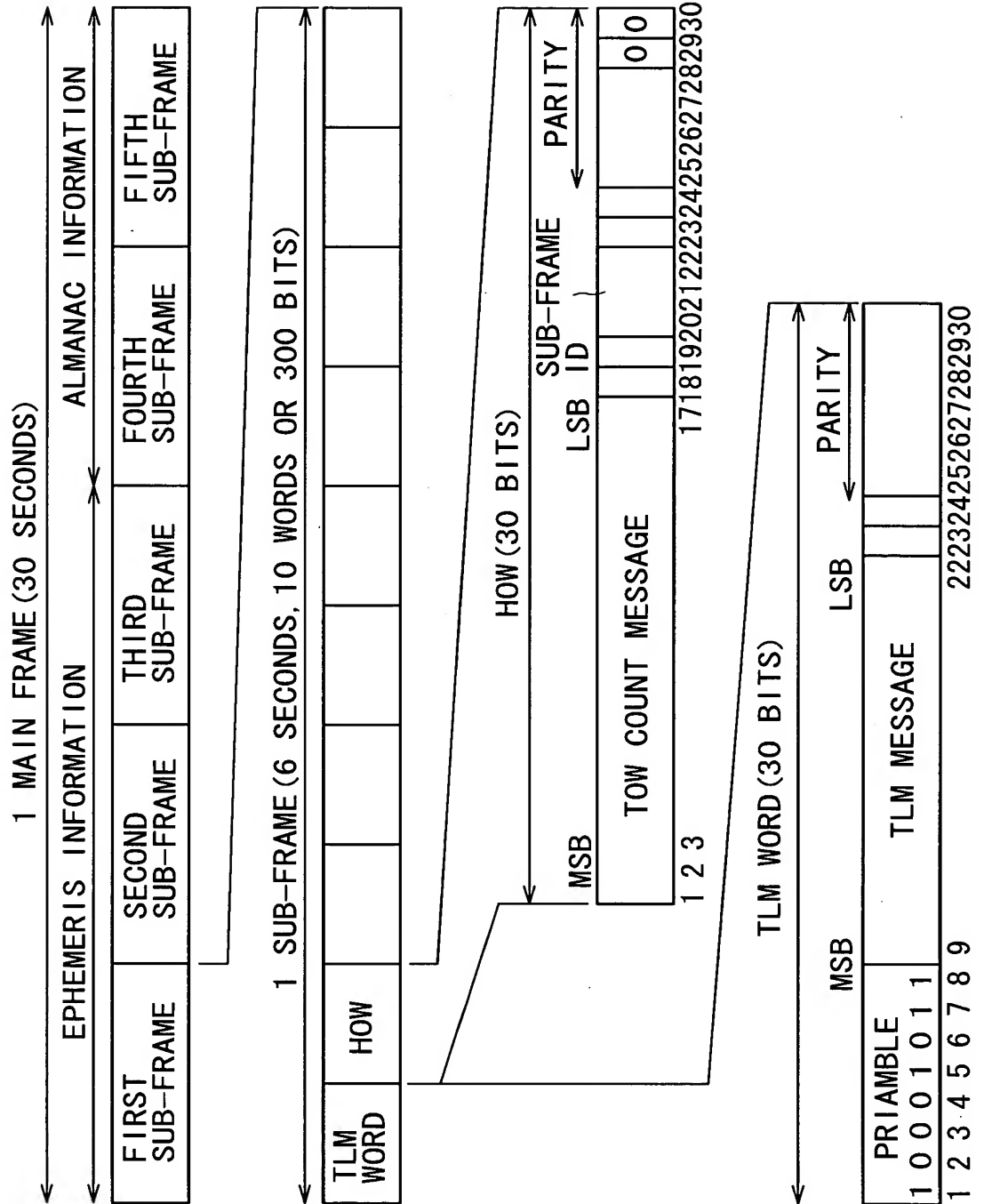
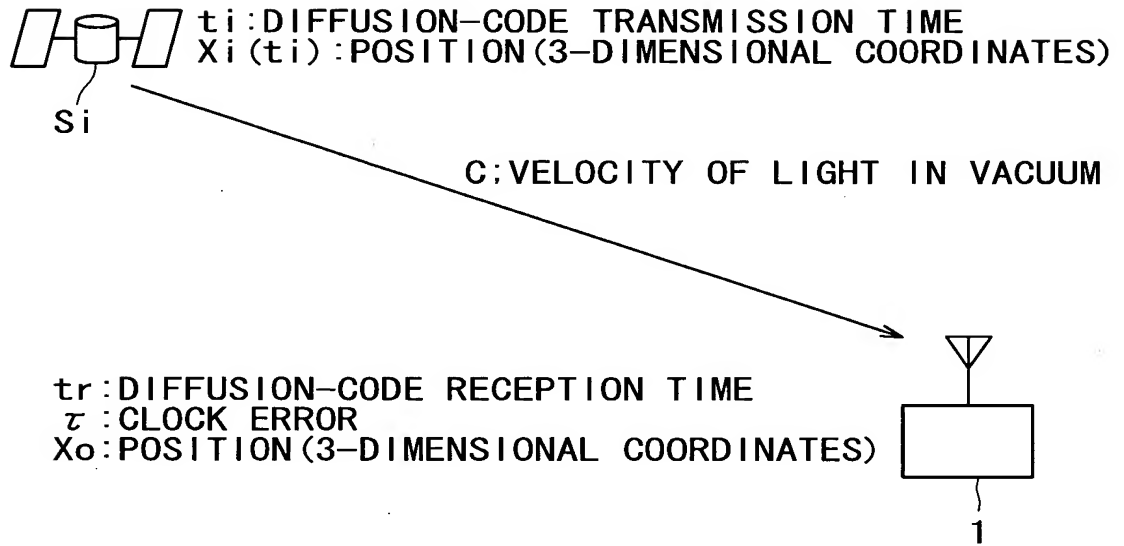


FIG. 21



F I G. 2 2 A



F I G. 2 2 B

$$|X_i(t_i) - X_o| - c\{(t_r - t_i) + \tau\} = 0 \quad \dots\dots (91)$$

$$X_i(t_i) = (x_i(t_i) \ y_i(t_i) \ z_i(t_i))^T \quad \dots\dots (92)$$

$$X_o = (x_o \ y_o \ z_o)^T \quad \dots\dots (93)$$

$$|X_1(t_1) - X_o| - c\{(t_r - t_1) + \tau\} = 0 \quad \dots\dots (91a)$$

$$|X_2(t_2) - X_o| - c\{(t_r - t_2) + \tau\} = 0 \quad \dots\dots (91b)$$

$$|X_3(t_3) - X_o| - c\{(t_r - t_3) + \tau\} = 0 \quad \dots\dots (91c)$$

$$|X_4(t_4) - X_o| - c\{(t_r - t_4) + \tau\} = 0 \quad \dots\dots (91d)$$

$$f_4(X_o) = |X_o| - |X_{oa}| = 0 \quad \dots\dots (95)$$

X_{oa} : APPROXIMATE POSITION OF RECEIVER